*Transform the function from time-domain
to frequency domain:

* used with non-Periodic signals.

time T.D F.T G(F)
domain 21t) F.T G(F)

inverse fransform

 $\frac{F.T}{G(f)} = \int_{-\infty}^{+\infty} 2(t) e^{-J_2TTft} dt$

 $\frac{1.F.T}{2(t)} = \int_{-\infty}^{+\infty} G(f) e^{tJ2\pi ft} df$

 $\theta = \omega t$ $= 2\pi f t$

II sec 3

Sheet #2

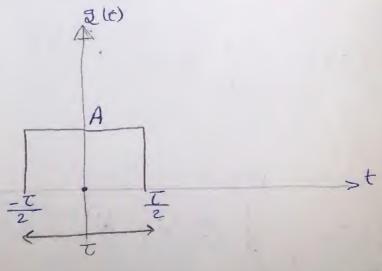
rectangular IT Find F.T for the -> rect Pulse shown > 17 * $2(t) = A \int \left(\frac{t}{\tau}\right)$

-: 213 7 trais 2) ses siè «

٣- عرون المستطيل

١- إرتناع المستطيل. ٥- عركز المستطيل

-: 0 > Util (3 c-A -> ارتباع المستطيل. المحرون الستعامل



-: rect کا نحدید مرکز ال O istalinde ag 1xt es vialing to aquero ق أى رقم نعتم عليه (بسط ومقام) @ نساوى البسط بلوعز للحوول على المركز.

Sec 3 2

$$G(F) = \int_{-\infty}^{\infty} 2(t) \cdot e^{\int 2\pi F t} dt$$

$$= \int_{-\frac{\tau}{2}}^{\frac{\tau}{2}} A - e^{-\frac{\tau}{2}} dt$$

$$=A.\frac{-J2\pi Ft}{(-J2\pi F)}\Big|_{-\frac{J}{2}}^{\frac{J}{2}}$$

$$=\frac{A}{\left(-J2\pi F\right)}\begin{bmatrix}-J2\pi F\frac{T}{2}\\ e\end{bmatrix}+J2\pi F\frac{T}{2}\end{bmatrix}$$

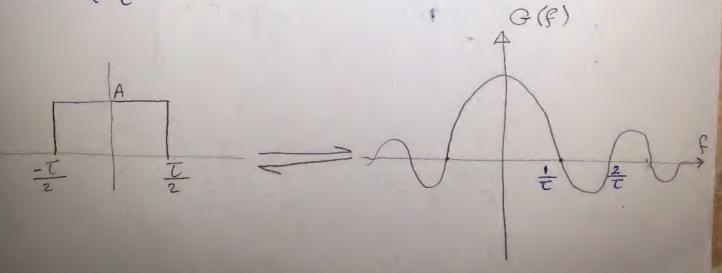
$$= \frac{A}{-J2\pi F} \begin{bmatrix} -J\pi F\tau \\ e \end{bmatrix}$$

$$\frac{\text{Note}}{\text{Cos}\,\theta} = \frac{\text{J}\theta}{\text{e} + \text{e}} = \frac{\text{J}\theta}{\text{c}} = \frac{\text{J}\theta}{\text{e} - \text{e}}$$

$$= \frac{A}{\pi f} \begin{bmatrix} + \sigma \pi f \tau & -\sigma \pi f \tau \\ - e \end{bmatrix}$$

Note

Arect
$$\left(\frac{t}{t}\right)$$
 = At sinc (FT)



sinc (o)
$$s = 1$$
, $\lim_{x \to 0} \frac{\sin x}{x} = 1$

$$f = 1,2,3...$$
 $f = \frac{1}{C}, \frac{2}{C},...$

Some important functions:

Qunit step functions:

$$u(t) = \begin{cases} 0, & t < 0 \end{cases}$$

$$u(t) = \begin{cases} \frac{1}{2}, & t = 0 \end{cases}$$

$$1, & t \neq 0 \end{cases}$$

- UH) - u(+) -->-1, t70 u(+t) u(-t) [2] signum fünetisn San(t) San(t) = 57-1 t<0

[6] sec = 3

$$S(t) = \int_{0}^{\infty} \infty t = 0$$

$$+\infty \int S(t) dt = 9$$

$$\int_{-\infty}^{+\infty} \int_{-\infty}^{\infty} S(t) dt = 1$$

a) Draw Q (t)

Aet

Aet

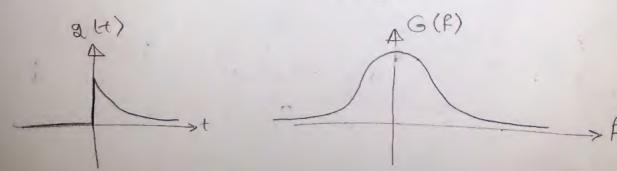
Au(t)

b)
$$\omega$$
 $G(f) = \int 2\pi f t$
 $-\infty$

$$= \int 2\pi f t$$

rect rect (Lizzal)

$$= \frac{-t(1+J2\pi f)}{-(1+J2\pi f)} |_{0}^{\infty}$$



$$|G(f)|_{5} = \frac{1}{\sqrt{1 + 4\pi^{2}f^{2}}}$$

$$|t| = \begin{cases} \frac{50!}{t^{70}} \\ +t \\ \frac{1}{t^{70}} \end{cases}$$

$$2(t) = e^{\alpha t} \qquad t = 0$$

$$t = 0$$

$$t = 0$$

$$G(F) = \int_{-\infty}^{+\infty} 2lt$$
 -J2TTFt dt

$$= \int_{-\infty}^{\infty} \int_{e}^{\infty} \frac{dt}{dt} - J2\Pi ft$$

$$= \int_{-\infty}^{\infty} \int_{e}^{\infty} \frac{dt}{dt} - J2\Pi ft$$

$$= \int_{-\infty}^{\infty} \int_{e}^{\infty} \frac{dt}{dt} - J2\Pi ft$$

tat e



$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left(\frac{1}{\alpha} - \frac{1}{3} \sum_{i=1}^{\infty} \frac{1}{\alpha} \right) dt + \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{1}{\alpha} \left(\frac{1}{\alpha} + \frac{1}{3} \sum_{i=1}^{\infty} \frac{1}{\alpha} \right) dt$$

$$\frac{e}{\alpha - J2\pi f} = \frac{-e(\alpha + J2\pi f)}{e(\alpha + J2\pi f)} = \frac{-e(\alpha + J2\pi f)}{-(\alpha + J2\pi f)} = \frac{e}{a}$$

$$G(f) = \frac{1}{\alpha - \sigma^2 \pi f} + \frac{1}{\alpha + \sigma^2 \pi f}$$

* Fourier transform Properties

هی مجوعه سه الخواجی تساعدنا می لیجاد (۲۰۰۲) لددال مجودلة بعلومیة دوال آخری معلومه و لیس عدم طریعه التکامل.

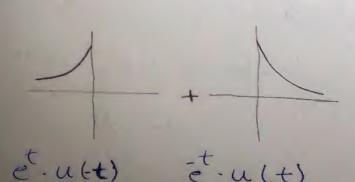
Let
$$g_1(t) \Longrightarrow G_1(f)$$

$$g_2(t) \Longrightarrow G_2(f)$$

$$\frac{1}{2} = \frac{1}{2} \frac{$$

A) Find F.T of
$$2(t) = \overline{e}^{1t}$$

 $2(t) = \overline{e}^{t} + \overline{e}^{t}$



$$\frac{e^{t} - u(-t)}{e^{t} - u(-t)} = \frac{1}{1 + J2\pi f}$$
 $\frac{e^{t} - u(-t)}{1 - J2\pi f}$

-susing Linearity

then
$$2(a-t) = \frac{1}{|a|} - G(\frac{f}{a})$$

Find F.T for 21t) = e -ult) $e^{\frac{1}{2}} = \frac{1}{1 + J_2 \pi f}$ u(t) (step) لات عبى النقالة الترجيدة عبرها (step) using time scaling at $\frac{1}{|a|}$ $\frac{1}{1+\sqrt{2\pi}f}$

14 Sec 3